

## Test 2 Review

1) Verify that the following is an identity:

$$\sin^2 x = \frac{1}{2}(1 - \cos 2x)$$

2) Verify that the following is an identity:

$$(\sin x + \cos x)^2 = 1 + 2 \sin x$$

3) Write as a sum (you can verify by graphing):

$$y = \sin 3m \cdot \cos m$$

4) Verify that the following is an identity:

$$\frac{\sin 2t + \sin 4t}{\cos 2t - \cos 4t} = \cot t$$

5) Solve the following to four decimal places:

$$2 \sin x = \cos 2x$$

6) Solve the triangle with sides:

$$a = 4m, b = 10.2m, c = 9.05m$$

7) Solve the triangle with the following:

$$\alpha = 122^\circ, \gamma = 18^\circ, b = 12km$$

8) Sketch the graph of:

$$r = 4$$

10) Sketch the graph of:

$$\Theta = \frac{\pi}{3}$$

11) Write the exponential equation in logarithmic form:  $32^{2/5} = 4$ 

12) Solve the equation for x.

$$e^{x^2+8} = e^{6x}$$

13) Find the domain, intercepts, and asymptotes of the logarithmic function **and** sketch its graph:

$$h(x) = \log_2(x - 4)$$

14) Approximate the logarithm using the properties of logarithms, given  $\log_b 2 = 0.3562$  and  $\log_b 3 = 0.5646$ .

$$\log_b(3/4)$$

15) Condense the expression to the logarithm of a single quantity.  
 $3 \ln(7) + 5 \ln(z - 9)$

16) Convert the angle measure  $65^\circ$  from degrees to radians. Round to three decimal places.

17) Find three values for  $\theta$  that make the statement true:

$$\theta = \left(\frac{1}{2}, \frac{\sqrt{3}}{2}\right)$$

18) Find the exact values for:

$$\sin \frac{5\pi}{2} =$$

$$\cos \frac{\pi}{6} =$$

19) Use the given function values and the trigonometric identities to find the exact value of each indicated trigonometric function.

$$\sin(\alpha) = \frac{12}{13}$$

$$\sin(\alpha) =$$

$$\cos(\alpha) =$$

$$\tan(\alpha) =$$

$$\cot(\alpha) =$$

$$\csc(\alpha) =$$

$$\sec(\alpha) =$$

20) Solve exactly for all values of Theta on  $[-2\pi, 2\pi]$  where  $\sin \Theta = 1$

21) Solve exactly for all values of Theta on  $[-2\pi, 2\pi]$  where  $\tan \Theta = -1$

22) State the period and amplitude for  $y=4\sin 3x$

23) Sketch the graph of  $y=\arcsin x$  and give the domain and range.

Period:

Amplitude:

24) Verify the identity:

$$\frac{\cos^2\left(\frac{\pi}{2} - x\right)}{\cos(x)} = \sin(x) \tan(x)$$

25) State the quadrant in which  $\theta$  lies when:

$$\sin \theta < 0 \text{ and } \cos \theta > 0$$

Use a calculator to evaluate the trigonometric function. Round your answer to four decimal places.

$$\sec 225^\circ = \underline{\hspace{2cm}}$$

26) Verify the identity:

$$9 \cos(t) + 9 \sin(t) \tan(t) = 9 \sec(t)$$

27) Verify the identity (Hint: try factoring):

$$9 \cos^2 \beta - 9 \sin^2 \beta = 9 - 18 \sin^2 \beta$$

28) Approximate (to three decimal places) the solutions of the equation in the interval  $[0, 2\pi)$ .

$$4 \tan^2(x) = 19$$

29) Solve the equation.

$$10 \cos^2(x) + 5 \cos(x) - 5 = 0$$

30) Verify the identity.

$$\sec(x) - \cos(x) = \sin(x) \tan(x)$$

31) Find the exact values of the sine, cosine, and tangent of the angle.  $\frac{11\pi}{12} = \frac{3\pi}{4} + \frac{\pi}{6}$

32) Solve for a triangle given

$$a = 51 \text{ m} \quad A =$$

$$b = \quad B = 20^\circ 30'$$

$$c = 41 \text{ m} \quad C =$$