

STAT 3631/5631 Homework

Applied Statistics and Probability for Engineers
Montgomery and Runger

Assignment 4

- a. Chapter 2: 117, 119, 121, 124.
- b. Chapter 3: 1, 3, 5, 9, 13.

$$\begin{aligned} 2-117. \quad P(B|A) &= \frac{P(A|B)P(B)}{P(A)} = \frac{P(A|B)P(B)}{P(A|B)P(B) + P(A|B')P(B')} \\ &= \frac{0.4 \times 0.8}{0.4 \times 0.8 + 0.2 \times 0.2} = 0.89 \end{aligned}$$

$$2-119. \quad (a) P = (0.31)(0.978) + (0.27)(0.981) + (0.21)(0.965) + (0.13)(0.992) + (0.08)(0.959) = 0.97638$$

$$(b) P = \frac{(0.21)(0.965)}{0.97638} = 0.207552$$

2-121. Let G denote a product that received a good review. Let H, M, and P denote products that were high, moderate, and poor performers, respectively.

$$\begin{aligned} a) \quad P(G) &= P(G|H)P(H) + P(G|M)P(M) + P(G|P)P(P) \\ &= 0.95(0.40) + 0.60(0.35) + 0.10(0.25) \\ &= 0.615 \end{aligned}$$

$$\begin{aligned} b) \text{ Using the result from part a.,} \\ P(H|G) &= \frac{P(G|H)P(H)}{P(G)} = \frac{0.95(0.40)}{0.615} = 0.618 \end{aligned}$$

$$c) P(H|G') = \frac{P(G'|H)P(H)}{P(G')} = \frac{0.05(0.40)}{1 - 0.615} = 0.052$$

Section 2-8

2-124. Continuous: a, c, d, f, h, i; Discrete: b, e, and g

3-1. The range of X is $\{0, 1, 2, \dots, 1000\}$

3-3. The range of X is $\{0, 1, 2, \dots, 99999\}$

3-5. The range of X is $\{1, 2, \dots, 491\}$. Because 490 parts are conforming, a nonconforming part must be selected in 491 selections.

3-9. The range of X is $\{0, 1, 2, \dots, 15\}$

3-13. The range of X is $\{0, 1, 2, \dots, 40000\}$